

Paired Sample T-test

Objective: Compare Means Between Two Dependent Samples

A researcher is interested in the effectiveness of a new drug to reduce LDL levels in men with high cholesterol. LDL levels of participants will be measured at the start of the study and after 3 months. A reduction in LDL level of 0.3 would be considered a clinically meaningful change. From pilot data, the standard deviation of the change in LDL levels is about 0.77. Power of 90% with a significance level of 5% is desired for the test.

Required Information	Inputs
What is the desired power for the test?	90%
At what significance level do you want to test your hypothesis?	5%
What difference do you want to be able to detect?	0.3
What is the standard deviation of the change in the response variable?	0.77
Is your hypothesis one-sided or two-sided?	Two-Sided

Effect Size will need to be calculated from the Mean Difference and Standard Deviation. This can be done by using the equation:

$$\text{Effect Size} = (\text{Mean Difference}) / (\text{Standard Deviation of the Change in the Response Variable})$$

Therefore, our Effect Size is:

$$\text{Effect Size} = (0.3) / (0.77) = 0.3896$$

Now input these numbers into our sample size calculator available at <https://sample-size.net/sample-size-study-paired-t-test/>



Sample Size Calculators for designing clinical research

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Calculators

CI for proportion

CI for mean

Means - effect size

Means - sample size

Correlation - sample size

Sample size for before-after study (Paired T-test)

Measure a continuous outcome y in each subject at the start and end of the study period. For each subject, calculate the change $\Delta = y_{\text{end}} - y_{\text{start}}$. Compare the mean value of Δ to 0. This requires the standard deviation S_{Δ} . The estimate of S_{Δ} should be based on data from other subjects who were followed for similar time periods.

Instructions: Enter parameters in the **green** cells. Answers will appear in the **blue** box below.

From the difference we want to be able to detect and standard deviation of the change in the response variable we can calculate the effect size: $0.3 / 0.77 = 0.3896$

Effect Size = Mean Difference / StdDev	α (two-tailed) =	5.0 %	Threshold probability for rejecting the null hypothesis. Type I error rate.
	β =	10.0 %	Probability of failing to reject the null hypothesis under the alternative hypothesis. Type II error rate.
	E =	0.3896	Effect size
	S_{Δ} =	0.7700	Standard Deviation of the CHANGE in the outcome. (If you don't know S_{Δ} , click here to calculate it.)

Calculate

1. Calculation using the T statistic and non-centrality parameter:

A value of $N = 43.0085$ gives the following calculations:

NCP = Non-centrality parameter = $\sqrt{N} * E/S_{\Delta} = 3.3182$.

DF = Degrees of freedom = $N - 1 = 42.0085$.

t_{α} = Inverse of the two-tailed T distribution given probability of $1-(\alpha/2)$ and DF of $42.0085 = 2.0181$.

$\text{Beta}(t_{\alpha}, \text{DF}, \text{NCP}) = 0.100010$. If N was calculated correctly, this should closely approximate your selected value of β , above.

The N thus calculated is rounded up to the next highest integer to give the group size.

Group size N: **44**

A total sample size of 44 is needed.

Example using the UCSF Sample Size Calculators for Designing Clinical Research (<https://sample-size.net/sample-size-study-paired-t-test/>)